

Digital Signal Processing
a **Computer Science Perspective**

Jonathan (Y) Stein



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To Ethel, Hanna and Noga

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